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Self-organised Aggregation in Swarms of Robots with Informed Robots

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Abstract. In this paper, we study a swarm of robots that has to select one aggregation site in an environment in which two sites are available. It is known in the literature that, in presence of asymmetries in the environment, robot swarms are able to perform a collective choice and aggregate in one among two possible sites, for example the largest of the two. We focus on an aggregation scenario where the environment is morphologically symmetric. The two aggregation sites are identical with only one exception: their colour. In addition, in the swarm only a proportion of robots, that we call the *informed* robots, possess extra information concerning on which specific site the swarm is required to aggregate. The rest of the robots are *non-informed*, thus they do not possess the above mentioned extra information. In simulation-based experiments we show that, if no robot in the swarm is informed, the swarm is able to break the symmetry and aggregates on one of the two sites at random. However, the introduction of a small proportion of informed robots is enough to break the symmetry: the majority of the swarm aggregates on the site preferred by the informed robot. Additionally, the swarm is also able to completely aggregate on one of the two sites when only 30% of the robots are informed, independently from the swarm size among those we considered. Finally, we analyse how the time dynamics of the aggregation process depend on the proportion of informed robots.

Keywords: swarm intelligence · swarm robotics · self-organisation · aggregation · informed leaders

1 Introduction

Swarm robotics is a sub-domain of a larger research area dedicated to the design and control of multi-robot systems [26, 4]. Swarm robotics is characterised by

the following distinctive elements: i) the use of distributed embodied control, that is, each robot has its own on-board control system in charge of determining the robot's behaviour; ii) local perception, that is, each robot can sense and communicate only within a given range using sensors and actuators mounted on its body; iii) the use of indirect communication: given that the robots of a swarm are "anonymous", any single agent can not selectively choose a specific message receiver, but rather communicate implicitly through modification of the environment in which they operate, by emitting sound or by generating other types of signal that are eventually detected by other agents.

Research in swarm robotics generally focuses on the design of individual control mechanisms underpinning a desired collective response, which emerges in a self-organised way from the interactions of system components (i.e., the robots and their environment) [4]. Examples of such collective responses are area coverage [19], chain formation [27], collective decision-making and task partitioning [23, 25, 29], cooperative transport [1], and collective motion [14].

One of the main building blocks in swarm robotics is collective decision-making, the ability to make a collective decision without any centralised leadership, but only via local interaction and communication. Several types of collective behaviours can be seen as instances of collective decision making [30, 31], including collective motion where robots have to agree on a common direction of motion, and aggregation where robots have to agree on a common location in the environment. In a seminal study illustrated in [10], the authors study collective decision making in the context of collective motion looking at what happens when *implicit leaders* are introduced. These special individuals, also called informed individuals, have a preferred direction of motion and they bias the collective decision in that direction. The rest of the swarm does not have any preferred direction of motion, nor is able to recognise informed individuals as such. The authors show that the accuracy of the group motion towards the direction known by the informed agents increases asymptotically as the proportion of informed individuals increases. Moreover, the authors show that larger the group, the smaller the proportion of informed individuals needed to guide the group with a given accuracy.

In swarm robotics, the framework of implicit leaders has been studied mainly in the context of collective motion [8, 13, 14]. Inspired by these works, we study the effect of implicit leaders in another collective behaviour strongly linked to collective decision-making: self-organised aggregation [9, 18, 2]. Aggregation processes are extremely common in biological systems [5], resulting in clusters of agents at common areas in the environment. Self-organised aggregation (i.e., an aggregation process not driven by exogenous forces) has been studied in a variety of biological systems [11, 20] and also implemented on distributed robotic systems [16, 15, 18]. Indeed, aggregation is often a necessity for many collective systems as it is a prerequisite for other cooperative behaviours [12, 28].

Aggregation has been studied as a best-of- n collective decision-making problem [30] in [17] and in [7]. In both studies, the authors have considered the presence of two circular aggregation sites in the environment, the only two areas where robots can stop, that are indistinguishable to the robots. In [17], the

authors considered two cases: in the first one, where the two sites have equal size, under special circumstances the swarm can break the symmetry and aggregate on one of the two sites at random; in the second one, where the two sites have different sizes, robots are able to collectively chose the biggest among the two aggregates. In a setting that is similar to the second one in [17], using a different model, the authors of [7] design a swarm able to select the smallest site that can host the entire swarm, rather than the biggest one.

Differently from the aggregation studies mentioned above, and analogously to the studies performed within collective motion [10], in this paper we introduce “informed” robots in the context of self-organised aggregation, and we study how they impact the aggregation dynamics. Informed robots are members of the swarm that have been informed a priori about the aggregation site to stop on, in an environment that offers multiple sites for aggregation. Apart from the preference on the site on which to aggregate, the behaviour of informed robots is controlled by exactly the same mechanisms of non-informed robots. The roles of informed robots is to influence the aggregation dynamics, in a very indirect way, since none of the robots has any means to discriminate informed from non-informed robots. We perform our study with a series of simulation experiments on the simplest possible scenario, represented by a circular arena with two aggregation sites: the desired one coloured in black, and the one to be avoided, coloured in white. The results of our simulations show interesting relationships between swarm size and proportion of informed agents, both on quality and speed of convergence on the desired aggregation site.

The rest of the paper is structured as follows. Section 2 describes the self-organised aggregation method used. In Section 3, we present the experimental setup and how we study the effect of informed robots. Section 4 presents the results of our study. Finally, in section 5, we discuss the significance of our results for the swarm robotics community, and we point to interesting future directions of work.

2 Methods

Each robot is controlled by a probabilistic finite state machine (PFSM, see also Figure 1a), similar to the one employed in [20, 2, 9, 6]. The robots’ controller is made of three states: Random Walk (\mathcal{RW}), Stay (\mathcal{S}), and Leave (\mathcal{L}). When in state \mathcal{RW} , the movement of the robot is characterised by an isotropic random walk, with a fixed step length (5 seconds, at 10 cm/s), and turning angles chosen from a wrapped Cauchy probability distribution characterised by the following PDF [21]:

$$f_{\omega}(\theta, \mu, \rho) = \frac{1}{2\pi} \frac{1 - \rho^2}{1 + \rho^2 - 2\rho \cos(\theta - \mu)}, \quad 0 < \rho < 1, \quad (1)$$

where $\mu = 0$ is the average value of the distribution, and ρ determines the distribution skewness. For $\rho = 0$ the distribution becomes uniform and provides no correlation between consecutive movements, while for $\rho = 1$ a Dirac distribution is

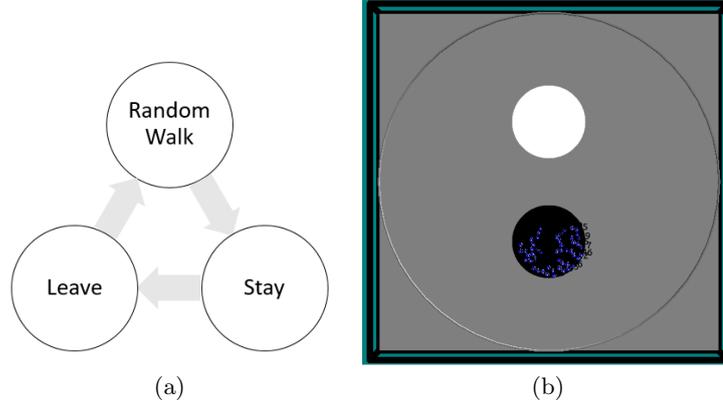


Fig. 1. (a) State diagram of the robots' controller. (b) The robots' arena with the black and white aggregation site.

obtained, corresponding to straight-line motion. In this study $\rho = 0.5$. Any robot in state \mathcal{RW} is continuously performing an obstacle avoidance behaviour. To perform obstacle avoidance, first the robot stops, and then it keeps on changing its headings of a randomly chosen angle uniformly drawn in $[0, \pi]$ until no obstacles are perceived.

A robot that, while performing random walk, reaches any of the two aggregation site, it stops with probability (P_{stay}). This probability is computed using the following function:

$$P_{stay} = 0.03 + 0.48 * (1 - e^{-an}); \quad (2)$$

with n corresponding to the number of other robots currently stationing on the site that are perceived by the robot currently deciding whether to stop or not; and $a = 2.6$. This function was first introduced in [6]. It interpolates the probability table considered in classical studies such as [20, 9]. Once the robot has decided to stop based on P_{stay} , it moves forward for a limited number of time in order to avoid stopping at the border of the site thus creating barriers preventing the entrance to other robots, and then transitions from state \mathcal{RW} to state \mathcal{S} . Once in state \mathcal{S} the robot leaves the aggregation site with probability P_{leave} . This probability is computed in the following:

$$P_{leave} = e^{-bn}; \quad (3)$$

with $b = 2.2$. This function was also introduced in [6]. A robot that decides to leave the aggregation site based on P_{leave} transitions from state \mathcal{S} to state \mathcal{L} . Both P_{stay} and P_{leave} are sampled every 20 time steps. When in state \mathcal{L} , the robot moves away from the site by moving forward while avoiding collisions with other robots until it no longer perceives the site. At this point, the robot transitions from state \mathcal{L} to state \mathcal{RW} .

In our model we consider two kinds of robots: *informed* and *non-informed*. Informed robots are agents that possess extra information on what is the site on which the swarm has to aggregate. Ideally, this extra information could be either generated by additional sensors, mounted only on informed robots, which allow these robots to perceive the quality difference between the two aggregation sites, or communicated by the experimenter with the intention to influence the swarm aggregation dynamics. In our simulated scenario, we consider aggregation sites in two different colours: black and white. Informed robots are aware that the task requires to stop only on the black site. Therefore, they ignore the white site, and only stop on the black site based on P_{stay} , as described above. Non-informed robots do not possess this extra information, therefore they can stop both on the black and on the white site based on P_{stay} , as described above.

3 Experimental Setup

In this set of simulations, a swarm of robots is randomly initialised in a circular area with the floor coloured in grey except for two circular aggregation sites one coloured in white and one in black (see Figure 1b). The task of the robots is to find and aggregate on the black site. Some of the robots are informed on which site to aggregate. The proportion of informed robots, henceforth denoted as ρ_I is systematically varied from $\rho_I = 0$ (i.e., none of the robots is informed on which site to aggregate) to $\rho_I = 1$ (all the robots are informed on which site to aggregate) with a step size of 0.1. We run three different experimental conditions, in which we varied the swarm size. As aggregation performance are heavily influenced by swarm density [6], in this paper we have decided to study scalability by keeping the swarm density constant. Therefore, the diameter of the area, as well as the diameters of the two sites, is varied as well. Table 1 reports a summary of our experimental conditions. In all conditions, the diameter of each aggregation site is large enough to accommodate all the robots of the swarm.

Each experimental condition can be divided in 11 groups which differ in the proportion of informed robots ρ_I . For each proportion ρ_I , we execute 200 independent runs. In each run, the robots are randomly initialised within the arena, and then they are left free to act according to actions determined by their PFSM for 10.0000 time steps. One simulated second corresponds to 10 time steps. Each run differs from the others in the initialisation of the random number generator, which influences all the randomly defined features of the environment, such as the robots initial position and orientation.

Table 1. Table showing the characteristics of each experimental condition.

experimental conditions	swarm size (N)	arena diameter (m)	aggregation site diameter (m)
1	20	8.3	1.8
2	50	12.9	2.8
3	100	19.2	4.0

We use ARGoS multi engine simulator [24]. The simulation environment models the circular arena as detailed above, and the kinematic and sensors readings of the Foot-bots mobile robots [3]. The robot sensory apparatus includes the proximity sensors positioned around the robot circular body, four ground sensors positioned two on the front and two on the back of the robot underside, and the range and bearing sensor. The proximity sensors are used for sensing and avoiding the walls of the arena. The readings of each ground sensors is set to 0.5 if the sensor is on grey, to 1 if on white, and 0 if on black. A robot perceives an aggregation site when all the four ground sensors return a value different from 0.5. Range and bearing sensors are used for inter-robot obstacle avoidance and for sensing the number of neighbours: the robots send a signal whenever they are stationing on a site. These signals are used by the robots to estimate the parameter n necessary to compute P_{stay} and P_{leave} .

4 Results

The main aim of this study is to look at how informed robots influence the aggregation dynamics in a task in which there are two possible aggregation sites, that can be differentiated only by informed robots. To do this, we used as performance indicator the proportion of robots aggregated on black site as $\Phi_b = \frac{N_b}{N}$ and on white site as $\Phi_w = \frac{N_w}{N}$ (where N_b and N_w are the number of robots aggregated on the black and white site, respectively) during the last 100.000 time steps of each run. The goal of the swarm is to maximise Φ_b and to minimise Φ_w . Note that $\Phi_b + \Phi_w \leq 1$ as it is possible that not all robots have aggregated in either site by the end of the run.

Prior to testing the effect of informed robots, we conduct a first set of experiments to validate our model. The model we used (see Section 2), is strongly influenced by the work of Garnier et al. [17]. According to this study, in presence of perfectly symmetrical aggregation sites, this aggregation model results in a symmetry breaking, whereby robots tend to chose one of the two sites at random. They aggregate in the chosen site, provided that the site is big enough to host the entire swarm. This symmetry breaking property is an essential feature of a self-organised aggregation method as it provides the positive feedback mechanism necessary for such behaviour. In order to test whether our model has this feature, we have executed experiments without informed robots in order to replicate the results in [17]. To calculate the strength of the positive feedback mechanism, we calculate the proportion of robots aggregated in the largest aggregate as $\max(\Phi_b, \Phi_w)$, independently on whether it is on the black or the white site. Results are shown in Figure 2 in form of frequency distribution. The graphs shows that, independently on the swarm size, the distribution looks multi-modal, with the highest peak at 1.0. This indicates that, for all considered swarm sizes, the swarm is able to create large aggregates around one of the sites at random.

We introduce informed robots and analyse how aggregation performance depend on their proportion ρ_I . The results are shown in Figure 3. We notice that for all swarm size, and when no robot is informed in the swarm ($\rho_I = 0.0$), both

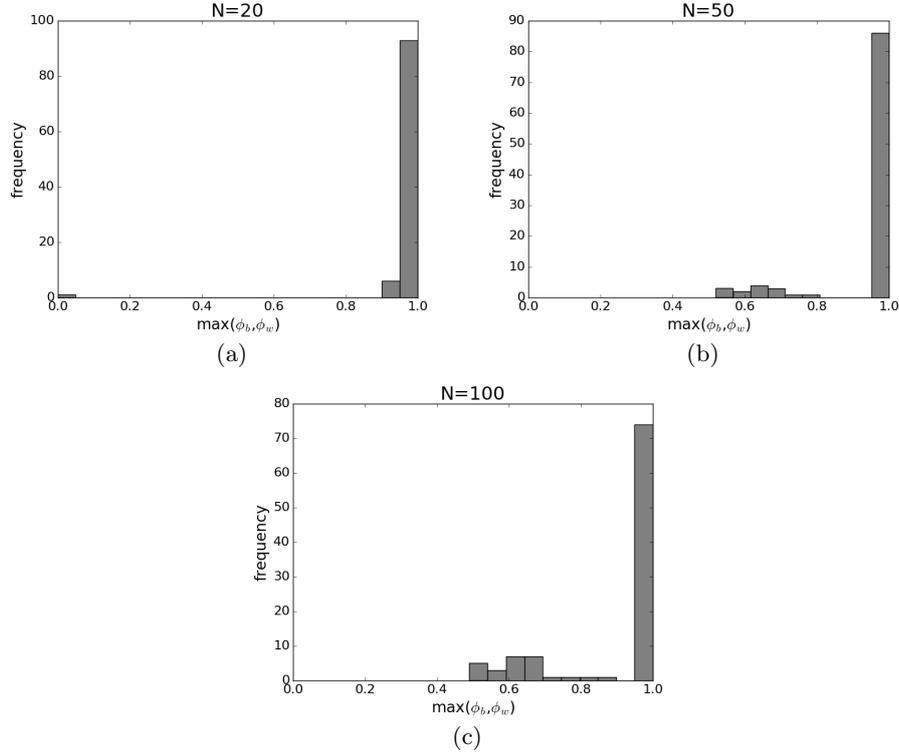


Fig. 2. Results of the experiments without informed robots ($\rho_I = 0$). The graphs show frequency histograms of the proportion of robots aggregating on the largest aggregate ($\max(\Phi_b, \Phi_w)$) for swarms of size a) $N=20$; b) $N=50$; and c) $N=100$.

Φ_b and Φ_w are centred around 0.5 with a strong variation. As we saw above, this may be explained by the fact that robots chose one aggregate at random under these conditions. Importantly, the introduction of as little as 10% of informed robots clearly breaks the equal-frequency bimodal aggregation dynamics between the black and the white sites and generates new dynamics that tend to bring the majority of the robots on the black site. Furthermore, all three graphs show a similar trend in which the higher the number of informed robots, the higher the proportion of robots aggregated on the black site. This trend is non-linear and reaches saturation at around $\rho_I = 0.2$ for $N = 20$ and $N = 100$, and for $\rho_I = 0.3$ for $N = 50$. With as little as 20% to 30% of informed robots, the totality of the runs finishes with more than 90% of the robots aggregated on the black site (see black boxes for $\rho_I = 0.2$ in Figure 3a and 3c, and for $\rho_I = 0.3$ in Figure 3b). For the smallest and the largest swarm size ($N=20$ and $N=100$, see Figure 3a and 3c) 20% of informed robots is enough to bring forth very robust and consistent aggregation dynamics that take the entire swarm on the black site.

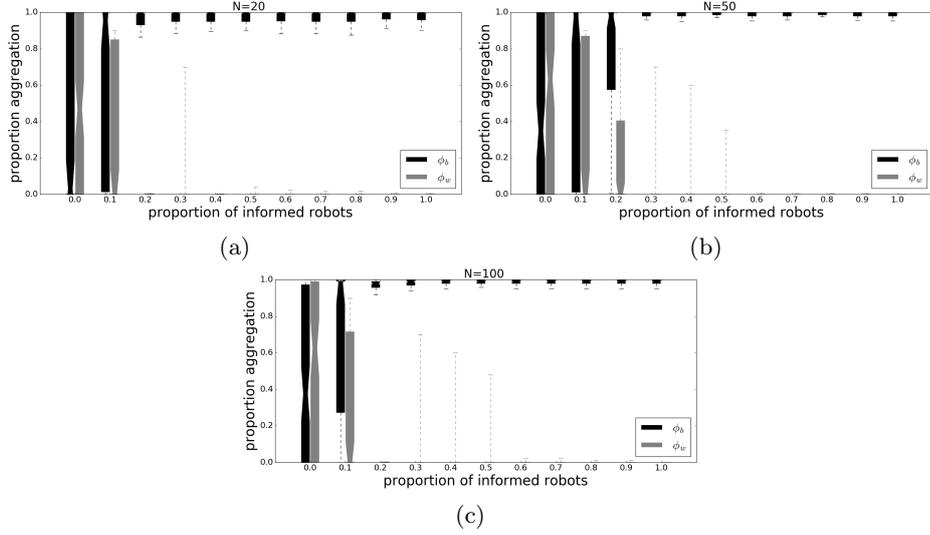


Fig. 3. Graphs showing the percentage of aggregated robots on the white site (i.e., Φ_w , see grey boxes) and on the black site (Φ_b , see black boxes) for swarms of size a) $N=20$; b) $N=50$; and c) $N=100$. In each graph, the x-axis refers to the proportion of informed robots.

For medium size swarm, similar robust and consistent dynamics can be observed when the proportion of informed robots is at least 30% ($N=50$, see Figure 3b). In summary, the above results indicate that with a proportion of informed robots varying from 0.2 to 0.3 of the entire swarm, it is possible to generate robust and consistent aggregation dynamics that take the totality of the swarm on a single site, in a task in which two possible aggregation sites are available.

The graphs in Figure 4 show details on the time dynamics of the aggregation process for three different values of ρ_I ($\rho_I = 0.1$ in Figure 4a, $\rho_I = 0.3$ in Figure 4b, and $\rho_I = 0.6$ in Figure 4c) and with the largest swarm size $N=100$. All figures feature a non-linear increase of the proportion of robots aggregated on the black site (i.e., Φ_b), which eventually reaches saturation. By increasing the percentage of informed robots, we initially observe that distribution of convergence values changes dramatically from $\rho_I = 0.1$ to $\rho_I = 0.3$. In the latter case, we already observe the almost totality of the runs converging to all robots aggregated on the black site, as the dashed top curve in Figure 4b tend to converge to $\Phi_b = 1$. When we increase ρ_I to 0.6, we observe that the variation between the different runs reduces dramatically while converging, and that all quartile of the distributions tend to converge to $\Phi_b = 1$. Additionally, we can also notice that, the higher the proportion of informed robots, the steeper the slope of the curve during both the first and the second phase. That is, by progressively increasing ρ_I the aggregation dynamics unfold in such a way that higher proportion of robots aggregated on the black site appear earlier during the run. To conclude, we can state that both

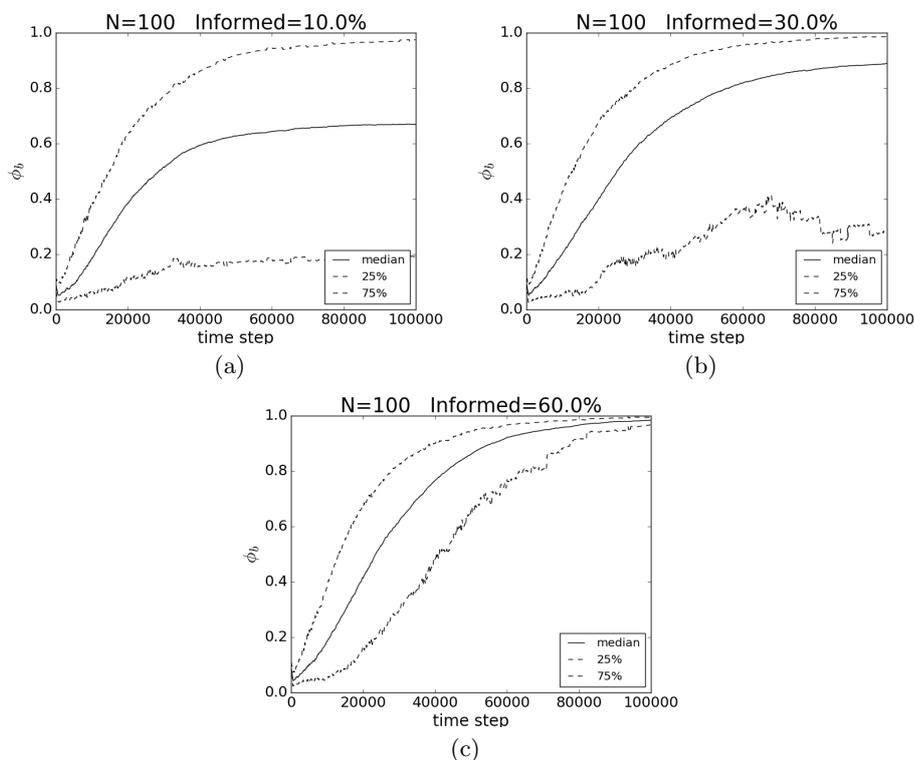


Fig. 4. Graphs showing the median (see continuous line), the first and third quartile (see dashed lines) of the proportion of robots aggregated on the black site (Φ_b) at every time step for 200 runs with swarm size $N=100$. In a) 10% of the swarm is informed; in b) 30% of the swarm is informed; in c) 60% of the swarm is informed.

speed (in terms of convergence) and accuracy (in terms of increase of percentage of robots aggregating on the desired site) of the aggregation process increase with increasing proportion of informed robots.

5 Conclusions

In this paper, we have contributed to the wider agenda of studying the role of implicit leaders in the context of collective decision making. We have focused on self-organised aggregation in the simplest possible scenario whereby two symmetrical but differently coloured sites are present. We considered a swarm of robots divided in two sets: informed robots, that possess extra information on which site the swarm has to aggregate, and non-informed robots which do not possess this extra information.

We conducted experiments using the ARGoS simulator in which we varied the proportion of informed robots from 0% to 100%. Our results show that, in absence of informed robots, robots can either split between the two sites, or break the symmetry randomly by aggregating in one of them. As soon as informed robots are introduced, the symmetry is instead immediately broken and increasingly more robots aggregate on the black site. When at least 20% to 30% of the robots are informed, the entire swarm aggregates on the black site, for all swarm sizes we have considered. We have also shown that the speed and accuracy of convergence is also strongly affected by the proportion of informed robots.

This study has the potential to be extended in many possible ways. First, in the context of aggregation, our next step will be to extend the study to more complex scenarios. We plan to test the discrimination capabilities of our swarms with informed robots in environments with more than two aggregation sites. These can include: environments with only one black (i.e., the correct) site and several white sites; environments with multiple black and white sites, in which we require the swarm to aggregate only on one of the black sites; environments with several different options (e.g. colours), which would correspond to a best-of- n problem with $n > 2$ [30]; scenarios where informed robots may have conflicting information about which is the best site and conflict resolution strategies need to be devised. Secondly, in our vision, we also plan to introduce implicit leaders in other collective behaviours. Finally, our framework can also have a practical relevance in the context of human-swarm interaction [22], whereby informed robots can correspond to robots that are controlled or tele-operated by humans, which would in turn introduce the human in the loop in order to study how humans can interact and control swarms of robots.

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